

Automatically Selecting and Optimizing Constraint Solver Procedures for Object-Constraint Languages

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Abstract

Object-constraint programming provides a design to integrate constraints with dynamic, object-oriented programming languages. It allows developers to encode multi-way constraints over objects and object collections using existing, object-oriented abstractions. These constraints are automatically maintained at run-time.

One original goal of the Babelsberg-family of object-constraint programming languages was to allow users familiar with the imperative paradigm to quickly and efficiently make use of constraint solver capabilities. Yet, practical problems often require careful selection of solvers to find good solutions (or any at all). Furthermore, solver performance can vary and while most solvers come with various optimizations, developers have to have a good understanding of the solving process to use these optimizations effectively. This, however, is difficult to achieve if the solver is automatically selected by the system.

In this work, we discuss three different implementations for automatic solver selection that we used in Babelsberg implementations. As a second step, we look at the performance potential of edit constraints that are available in some solvers such as Cassowary or DeltaBlue, and how they can be applied automatically to improve solver performance. We argue that these techniques make object-constraint programming more practical by improving the quality and performance of solutions.

Categories and Subject Descriptors D.3.3 [Programming Languages]: Language Constructs and Features—Constraints

Keywords Constraints, Incremental Re-solving, Object Constraint Programming, Constraint Imperative Programming, Babelsberg

1. Introduction

Babelsberg [6] is a design to integrate constraints into object-oriented languages in a way that allows programmers to dynam-

ically create and satisfy constraints on objects. The design is a strict extension of the object-oriented semantics of the underlying host language [8]. Babelsberg uses object-oriented method definitions to define constraints rather than a domain-specific language (DSL) [17, 20]. As a consequence, constraint expressions in Babelsberg respect encapsulation and can re-use object-oriented abstractions. The design also supports solver features such as constraint priorities [3] and incremental resolving [11], and can use multiple cooperating constraint solvers to search for solutions [7].

Examples for application domains where constraints can be particularly useful are physical simulations and animation, load balancing, data structure repair, and puzzle solving. For example, creating an imperative implementation of a Sudoku game works well for the graphical parts and user interaction, that is, for describing what should be displayed and what should happen when the user provides input. But spelling out how even a naive Sudoku solver works in object-oriented code still requires dozens of lines of code. Using the Babelsberg design and constraints, however, allows the user to describe the desired state that a valid Sudoku should have using ordinary objects and imperative methods.

```
1 always {  
2   sudoku.cells().all? { |c| 1 <= c && c <= 9 } &&  
3   sudoku.rows().all? { |r| r.all_different? } &&  
4   sudoku.columns().all? { |c| c.all_different? } &&  
5   sudoku_boxes().all? { |b| b.all_different? }  
6 }
```

Consider the above code listing. The predicates are valid Babelsberg code (implemented on top of Ruby), and assert that all cells of a Sudoku must have numbers between 1 and 9 and that all rows, columns, and 3x3 boxes in the Sudoku must not contain duplicate numbers. The constraint is introduced using the `always:` keyword, and uses ordinary object-oriented methods such as `all?`, `all_different?`, or `<=`. The Babelsberg design defines how to translate these expressions into a form ready for consumption by a constraint solver, and how the solution is fed back into the program state. This frees the developer from writing or maintaining the code for the solving itself. The only two conditions on constraint expressions are that they must return a boolean and that they must be free of side-effects [8].

An incomplete aspect of the original Babelsberg design was that it allowed multiple constraint solvers to be used cooperatively to solve constraints, but provided only minimal guidance to developers for deciding which solvers to use. Users who were not familiar with the capabilities and limits of the various available solvers of-

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MODULARITY Companion'16, March 14–17, 2016, Málaga, Spain
ACM. 978-1-4503-4033-5/16/03...
<http://dx.doi.org/10.1145/2892664.2892671>

ten resorted to trial and error find a working combination of solvers for a particular problem. Since it is in general much easier to state constraints than to solve them, practical constraint solvers restrict themselves to a useful subset of constraints in a particular domain for efficiency. This is apparent in many popular solvers: the Cassowary solver [1] can efficiently solve multi-way linear equations on floats using the simplex method; Z3 [4] is an SMT can numerically solve for reals, integers, booleans, as well as record data types; Kodkod [24], Z3, and Ilog [19] can enumerate solutions; and DeltaBlue [10] can solve multi-way constraints using local propagation. An even more restricted approach is to only consider one-way constraints that can compute an output value given new inputs, but not vice versa (e. g., [14, 18]). These restrictions must be considered when choosing solvers for a concrete set of constraints. In this work we discuss three different implementations for automatic solver selection that we used in the practical Babelsberg implementations.

These problems are also present in related approaches that combine constraints with general-purpose, imperative languages such as the earlier constraint-imperative programming (CIP) language Kaleidoscope [16] or Rosette [23], a solver-aided language based on Racket. In the former, the user has no control over which solver is chosen — adding a solver requires the language implementer to extend the solver-selection procedure to decide which solver to use. In Rosette, solvers can be added by users of the language, but users also have to manually specify which solver to use for a particular problem.

Even if a working solver is found for a concrete set of constraints, it may not be optimal in terms of performance. Although solving strategies such as incremental re-solving [11] and re-ordering of constraint declarations can improve performance of some solvers and are available in Babelsberg implementations [6], these optimizations have to be applied explicitly and are specific to particular solvers. Furthermore, the Babelsberg semantics treats the solver as a black box, and thus does not include a principled way of utilizing such optimizations [8]. In contrast, modern imperative language runtimes apply a growing number of optimizations automatically in a principled manner — either at compile-time or using just-in-time (JIT) compilation techniques — so that even unoptimized code provides good performance. To apply these techniques to constraint solving, we look at the performance potential of edit constraints in Babelsberg, and propose strategies to apply them automatically to improve solver performance.

Surprisingly, these automatic optimization strategies are not commonly applied to constraint solvers — as far as we know, there are no constraint solvers optimized for interactive use that optimize their own data structures. Thus, the optimization strategies we propose here can also be beneficial to the Cassowary and DeltaBlue solvers when used in other contexts. Additionally, our results indicate that further research into the optimization potential for constraint solvers and their data structures is warranted.

The contributions of this work are:

- Three practical implementations for automatically selecting a constraint solver given a concrete set of constraints.
- A novel application of JIT-compiler techniques to the Cassowary and DeltaBlue constraint solvers to improve solving performance transparently.

2. Automatic Solver Selection

Given that multiple solvers can be used cooperatively with the Babelsberg design, we need to figure out which solver to use for which constraint. Consider again the Sudoku constraints from page 1. These constraints are in the domain integers, and use pairwise inequalities. To solve them requires a constraint solver that can deal

with inequalities over integers. Either the developer or the system must decide which solver is capable of solving these constraints and use it. In this section, we present different heuristics for having the system select a solver automatically and present their trade-offs.

The solvers in the ThingLab [2] constraint programming system as well as from the Kaleidoscope constraint-imperative programming system [9] were automatically selected based on the type of constraint that was handed to it. In these languages, however, the set of available constraint solvers was fixed. More importantly, each solver had capabilities that the others lacked, and thus many constraints could clearly only be handled by one particular solver. The algorithm which determined how the constraints were added to the solvers only had to check for these specific capabilities of the solvers, and could be optimized easily. Such an algorithm is not possible with the Babelsberg design, however, since we do not know in advance which capabilities the solvers have, and the set of solvers can be extended by the user. Even worse, we may want to use different solvers with exactly the same capabilities, but that have different characteristics with regards to performance or solution quality.

The simplest approach at assigning a constraint to a particular solver would be to let the developer do it. Each constraint must then be annotated with the correct solver to use in the source — if the selection is incorrect (i. e., assigning the constraint to a solver which cannot solve it) or not ideal (i. e., using a general purpose problem solver when a specialized algorithm exists), the system does not attempt to correct the problem. However, this simple approach is undesirable. Object-constraint programming (OCP) is supposed to provide convenient access to constraint solving for imperative programmers, thus it is inconvenient to expect each user to have to learn about the capabilities and trade-offs between the different solvers before using them. Instead, manual annotation should be the fallback if the system is unable to select the ideal solver in a situation. This fallback is available in all Babelsberg implementations, but the implementations use different default strategies for selecting the solver if none is explicitly specified.

2.1 Eager Selection by Type

This is the selection mechanism implemented in Babelsberg/R. The mechanism specifies which solver to use per class, ignoring any relations between variables. To select a solver, the virtual machine (VM) sends the `for_constraint` message to each variable value encountered during constraint construction. User code can add solvers to the system by dynamically adding a `for_constraint` method to those classes for which the solver is applicable, making use of Ruby’s open classes. This method should return a solver-specific variable wrapper object that implements a subset of the interfaces that the solver can reason about. For example, the Cassowary solver extends the Float class:

```

1 def for_constraint(name)
2   v = Cassowary::Variable.new(name: name, value: self)
3   Cassowary::SimplexSolver.instance.add_stay(v)
4   v
5 end

```

This method creates a new variable, adds implicit, low-priority stay constraint (to instruct the solver not to change the variable value unnecessarily, and returns the solver-specific variable object. The VM’s solver object then sends messages to this object instead of the Float object in the context of the constraint execution.

When executing a constraint expression, the system determines the most specific dynamic types of each variable that it encounters. As long as no solver is selected for the current constraint, the system sends a solver selection message to the object to ask which constraint solver should be used for it. If the object does not understand the message, this indicates that no solver declared that it can

handle this type of object. If the object responds with a solver, the constraint is immediately assigned to that solver. Any further variables that are encountered are now interpreted with this solver. If they happen to be of a type that the solver can handle, they are normally represented as variables. If they are not, their current value will be used as if it had been annotated as read-only in the constraint expression. The solver will be able to use the value of the variable but not write to it, but when the variable changes, the updated value is passed to the solver.

If during the execution of the constraint expression no solver is selected, the constraint is taken as-is: if it is already `true`, no further action must be taken. When any of the variables that participate in the constraint change, the expression is re-executed using this same algorithm. If the expression returns `false` and no solver is selected, it is treated as unsatisfiable. In either case, a practical language should provide an appropriate warning to users, informing them that no solver could be found for a constraint involving the dynamic types that were encountered.

This selection algorithm is simple and fast. Constraints that deal with few types can quickly be assigned to the correct solver. However, the algorithm is brittle for constraints that include multiple types that each should be handled by a different solver. Consider the following example:

```

1 s = "Hello"
2 n = 5
3 always { n == s.length() * 2 }
4 always { s.length() * 2 == n }
5 n = 10

```

Suppose we have a local propagation solver that can deal with equalities over strings and numbers, but not arithmetic, and one that can solve linear equations over reals, but does not support strings. The two constraints in line 3 and 4 should be idempotent and it should be irrelevant in which order they are defined or solved.

The first constraint will be handed to the linear arithmetic solver, since we encounter the number `n` first during constraint construction mode (*ccm*). The solver will treat the string as a constant, and is thus forced to use the return value of the method `s.length()` to update `n` to 10. The second constraint will be handed to the local propagation solver, since we encounter the string `s` first. The constraint is already satisfied, so nothing needs to be done.

When we execute the assignment on line 5, the order in which the solvers are called to solve these constraints matters. We must first call the local propagation solver to update the string length. If we call the linear arithmetic solver first, it will give up and treat the constraint as unsatisfiable, since it cannot manipulate the string to make it longer. This can lead to confusing cases where the system will say a set of constraints is unsolvable, but a simple re-ordering of operations in the constraint expressions will make it work.

2.2 Selection by Preference

This is the selection mechanism employed in Babelsberg/S [12] and the original Babelsberg/JS implementation [7]. If the set of constraints that two or more solvers can solve is not empty, it may be desirable to always give preference to one solver over another, to avoid issues where the solver surprisingly changes when a constraint expression is refactored. To assign preferences, the system maintains a list of solvers implicitly ordered by preference. This list may be generated or supplied by the user. In either case, the list of solvers should be created early in the execution of the program and, once the first constraint has been created, it should only be possible to append, not remove or re-order solvers.

Instead of executing the constraint expression just once, it is executed in *ccm* once for each of the available solvers. The first solver that is able to work with at least some of the variables

that participate in the constraint is selected and the constraint is assigned to it. Executing the constraint expression multiple times is safe due to our requirement on it being free of side-effects.

For the above example, suppose that the arithmetic solver is preferred over the local propagation solver. In this case, both constraints will be assigned to it. This means, however, that the assignment on line 5 now becomes unsatisfiable! While this may seem like a strong restriction on the kinds of programs that can be written in this manner, we consider it preferable over the potential surprise that the two constraints above, even though they trivially express the same equality, are assigned to different solvers. In this scenario, the constraint system will always be unsatisfiable, regardless of how we refactor the two constraint expressions. To make the program work, the user should manually select the local propagation solver in this case, or else re-order the solvers to give preference to the local propagation solver at the beginning of the execution.

2.3 Heuristic Selection

Babelsberg/JS now implements some heuristics for solver selection. If no explicit solver was selected, the constraint is handed to multiple solvers in parallel. In Babelsberg/JS, each solver can declare capabilities, such as which types and operations it supports. Based on an initial analysis of the types and operations encountered in the dynamic extent of the constraint expression, solvers are filtered, and the remaining solvers all run to solve the constraint. The solvers to finish without error are compared first for accuracy of the result (which might be application specific) and then performance to select the final solver. Currently, no further heuristics are implemented, but the order of the trade-off (performance versus accuracy) can be swapped by the user.

The preferential solver selection presented before is already heuristic: it selects the first solver that can work with at least some of the variables that participate in the constraint. This heuristic is easily extended. An obvious extension is to select the first solver that can deal with the *most* variables, and go by preference only in case of a tie. There are more such extensions that make sense in this decision procedure. As described above, there may be solvers that have exactly the same capabilities, and that only differ in their performance or in the quality of their results.

Some of the solvers' properties, such as performance and the quality of the result, can be determined automatically. For others, this solver selection procedure requires solvers to come annotated with *capabilities*, such as the types and operations it supports, for which theories it is complete or incomplete, or whether it supports finite as well as infinite domains.

A simple example, which the preferential selection can already decide, is a constraint on two strings and the choice between a finite domain solver and an local propagation solver:

```

1 x = "Good Morning"
2 y = "G'day"
3 always { x = y }

```

We can tell from the types that the simplex solver will not be able to find a solution to this constraint and that we should pick the local propagation solver.

However, even a slightly more complex example may make our decision much more difficult. Suppose we hand the following constraint over the reals to both a simplex solver like Cassowary and a relaxation solver:

```

1 a = 2.0
2 b = 2.0
3 always { a * a = b }

```

Again reject the simplex solver, this time because it is not equipped to deal with non-linear equalities. The relaxation solver, on the

other hand, approximates a solution to this constraint by linearizing it, but it would be an approximation only. More worrisome is that the solving algorithm can diverge, so even if this constraint can be solved once, it may not be possible if we change either a or b too much in one step. Suppose a relaxation solver approximates the solution $a \mapsto 2.0$ and $b \mapsto 3.999999999998$ for the above constraint; because the relaxation method using numerical approximation, it is prone to round-off errors. If we have a solver like Z3 available, we might want to select it instead, both for higher precision, and because the solving theory is more robust (albeit not complete) for non-linear arithmetic over the reals. However, Z3 may pick another (valid) solution $a \mapsto 1.4$ and $b \mapsto 1.96$. This solution means that the sum of the changes to the variables is smaller than with the relaxation method, but for some applications, we may prefer a solution which modifies the least number of variables instead.

Our heuristic selection attempts to weigh these different criteria. As in the selection by preference, we execute the constraint expression once for solver, and in addition we let each solver solve the constraint once, but without updating the environment and heap with the solution. Using the preference and the below heuristics in conjunction, we can then select the best solver and add the constraint to it. As constraints are added, we regularly re-evaluate the metrics for existing constraints to check if they should be moved for better performance or better results. Similarly, when a constraint becomes unsatisfiable, but the current solver is annotated as being incomplete, we also re-evaluate the metrics to search for another solver.

Precision As an example, Cassowary is complete for linear equalities over reals, but its implementation uses float values to represent reals, so a concrete solution may suffer from round-off errors. Similarly, although the Z3 real theory works on reals of arbitrary precision, these reals will be represented in many languages as finite-precision floating point numbers, so again round-off errors may occur. The precision of the results these solvers produce may thus differ in practice, and could be considered as part of the solver selection.

Variable Changes Another property that may impact the quality of the solution is how the solver implementation affects the selection of solutions when multiple solutions are available. Although stay constraints are part of the semantics to ensure that any solution is close to the previous state of the system, there are often multiple possible solutions that satisfy this property. Which solution is selected is usually an artifact of the solver implementation. However, problems such as the split-stay problem may make some solutions still more desirable than others, and solvers which avoid it may be preferable over those that do not. Similarly, solvers that change multiple variables, but achieve a small squared distance from the previous state of the system may be more or less suited to a particular problem than those that change few variables, but those by a larger amount.

Dimensionality Besides the types of variables, the operations on them and how they are connected also play a role. Cassowary can only solve linear equations, while a relaxation solver can find solutions for higher dimensional arithmetic. Thus, the operations and associated operands within a constraint expression must be considered to select the solver.

Completeness Another issue arises with incomplete theories. SMT solvers, for example, require the different partial solvers within to be convex for the decision procedure to be complete. For example, the theory $(\mathbb{Z}, +, =)$ (addition and equality over the whole numbers) is convex, but $(\mathbb{Z}, +, \leq)$ is not — a constraint involving inequalities over the integers may be satisfiable for a specific set of values, but another set of values may make it simply

too hard for the solver. In that event, another solver (e. g., using a form of relaxation) may be able to approximate a solution and the constraint should be moved to that solver.

Performance Depending on the implementation, solvers may differ significantly in both base performance and complexity in required memory as well as time. As constraints are added during the execution of a program, a solver that is fast for few constraints may, due to higher complexity, become slower than a constraint with worse base performance but better complexity. A selection algorithm can take into account how fast a solver was able to satisfy a constraint, and continues to monitor solvers to notice drops in performance when constraints are added.

Each of these mechanisms has proven useful in practice to help developers not familiar with constraint solvers to use constraints in Babelsberg. When they do not work, however, the resulting confusion can impede development. Regardless of the chosen strategy, we believe that communicating the strategy and how the system arrived at a selection of solvers for a particular constraint is key to making them useful.

3. Fast Incremental Constraint Solving

Performance of the solving algorithm itself is important for Babelsberg languages. This is particularly apparent when few variables change with high frequency and constraints have to re-satisfied in response, for example, when a graphical object should follow the mouse cursor.

Not all constraint solvers are developed to provide good performance for interactive applications, being used primarily for proofing or model finding [4]. However, of the ones that are used interactively, some solvers have explicit support for re-solving in case of state changes with good performance. To that end, Freeman-Benson, Maloney, and Borning introduce the notion of *edit constraints* and incremental re-satisfaction [11]. Their work is based on the observation that user input is usually restricted to modify only small parts of the constraint graph at a time, for example modifying 2d coordinates when moving the mouse or modifying a string by entering one character at a time.

Both DeltaBlue and Cassowary treat stay and edit constraints specially, allowing very fast incremental re-satisfaction of a collection of constraints as new edit values stream into the system (and the weak stay constraints provide basic stability). For DeltaBlue, this involves pre-calculating the execution plan from the edit variables. For Cassowary, the Simplex tableau is set up so that it can be efficiently re-optimized given new values for the edit variables. Unfortunately, at least for Cassowary, preparing the solver for fast incremental re-solving of a few variables requires some re-organization of the tableau, and solving for other variables also becomes slower as a result. This requires developers to anticipate whether a variable will only change more or less often, and use the appropriate interface if they want to achieve the best performance.

The `edit` method provided as part of Babelsberg/R adds edit constraints and repeatedly updates them with values from a stream running in a separate thread. In Babelsberg/JS, to support edit constraints within a single thread, the `edit` method returns a callback to input new values into the solvers, rather than taking a stream of values. Babelsberg/S currently does not support edit constraints.

Since the language design supports cooperating solvers, the solvers have to provide a specific edit constraint application programming interface (API). If a variable is added to an edit constraint, but we dynamically discover that it is used in a solver which does not support the edit constraint API, a runtime exception is generated. Upon calling the `edit` method, the following methods are called on the solvers and the supplied variables, in order:

prepareEdit is called on each solver variable. In this method, variables can prepare themselves for editing. In Cassowary, for example, this would call the `addEditVar` method on the solver with the variable as argument. For DeltaBlue, this creates an `EditConstraint` on the variable and adds it to the list of constraints.

beginEdit is called once for each solver participating in the edit before the callback is returned. In Cassowary, this initializes the edit constants array and prepares the solver for fast re-solving when these constants change. In DeltaBlue, the solver generates an execution plan to solve the constraints starting with the `EditConstraints` as input.

resolveArray is used to supply each solver with the new values and update the object's storage (so other observers and hooks around the values still work). Because the solver's execution plan is fixed for the duration of an edit, we disallow creating new edit callbacks before the current edit has finished. When new constraints are created, the execution plan may also become invalid, but we do not enforce invalidating the edit callback in this case.

finishEdit is sent to each solver variable when the edit stream ends or the callback is called without arguments. Cassowary variables do nothing here, DeltaBlue variables remove their `EditConstraints` from the solver.

endEdit is called once for each solver to reset the solver state.

To use, for example, Cassowary as the solver, all edit variables must be Floats (e. g., the x and y values of a point), but we also want to do this in an object-oriented way that respects encapsulation. To support this, the client passes an array of method names for the return values that should be updated in the edit constraint (e. g., x and y for a point — those values may be calculated or direct accessors). The system creates fresh edit variables, and adds an equality constraint to the return values of the methods. Thus, the internal storage layout of the class is not visible to the programmer from outside the object, because the equality constraint is simply asserted on the results of message sends using the `always` primitive.

In the following example, the mouse locations or the mouse point might store their x and y values directly, or might be points represented using polar coordinates. In either case, the edit constraints apply to the return values of their respective x and y methods:

```
1 edit(stream: mouse.locations.each,  
2   accessors: [:x, :y]) { mouse_point }
```

In a DeltaBlue-specific edit method, the edit constraints returned could be simpler, since DeltaBlue local propagation methods can apply to user-defined objects such as points, not just to floats. The point would be simply updated rather than dealing with its x and y coordinates separately, and the data flow plan would update the objects constrained to be equal to the point that represents the mouse location.

Benchmark Results

To quantify the impact of edit constraints, we used an example from Kaleidoscope'93 [15] and adapted it to our Babelsberg implementations. In this example, the user drags the upper end of the mercury in a thermometer using the mouse. However, the mercury cannot go outside the bounds of the thermometer, even if the user tries to drag it out. Additionally, a gray and white rectangle on the screen should be updated to reflect the new mercury position, and a displayed number should reflect the integer value of the mercury top. Refactoring the imperative version for Babelsberg makes it more general, so the comparison is biased towards the imperative code. However,

this example demonstrates the performance impact if an imperative program is refactored with the goal to make it more readable, not more general.

Note that the object-constraint version may be written in two ways: one that is more like the imperative version and assigns new mouse locations in a loop; and a more constraint-oriented version that declares `mouse.location_y` as an edit variable that triggers incrementally re-satisfying the constraints. The latter is expected to be much faster, as Cassowary can just re-optimize a previously optimal solution.

In this set of benchmarks we only include Babelsberg/R and Babelsberg/JS, since we did not implement edit constraints in Babelsberg/S. The results are presented in Figure 1. The benchmarks were run on an otherwise idle Ubuntu 14.10 system using an Intel i5-2520M CPU forced to a constant clockspeed of 2.5 GHz with 16 GB of RAM. Benchmarks were run a varying amount of iterations (given in the charts) depending on the benchmark, and each benchmark run was repeated ten times, with the mean and standard deviation shown in the results where appropriate.

For both implementations, the hand-coded imperative version is clearly the fastest. However, it is also the longest, hardest to understand, and hardest to prove correct. It is also clear that the purely declarative versions are generally too slow to be used in an interactive application: in both cases, the system could re-satisfy constraints less than once per second, which is not enough to smoothly follow mouse movement and update the screen. Although using edit constraints is still an two to three orders of magnitude slower than pure imperative code, it is fast enough to re-satisfy constraints in an interactive application and still provide smooth display updates.

4. Automatic Edit Constraints

We have shown in Section 3 that edit constraints can significantly improve the performance of constraint solving and in some cases make the use of constraint solving feasible in the first place. However, using edit constraints directly requires developers to know about them, understand where they are useful, and to adapt the source code to create edit constraints.

Automatic edit constraints (just like our integration of state and object-oriented behavior with constraint declaration, or the architecture for cooperating solvers and solver selection heuristics) support the goal of Babelsberg to make constraints a useful tool for developers not familiar with constraint solvers. Rather than requiring object-oriented (OO) developers to learn about incremental solvers, in Babelsberg we have added heuristics for two solvers, DeltaBlue and Cassowary, to recognize variables that change frequently and use automatically apply incremental re-satisfaction to speed up solving.

The solving process of DeltaBlue when a variable is assigned involves creating a new equality constraint, creating an execution plan, executing that plan to solve the constraints, and finally to remove the equality constraint and the associated plan. As a simple optimization heuristic, we can keep the last n equality constraints and plans in a cache; if one of the n variables changes again, we can just update the equality constraint and re-use the execution plan, rather than re-creating it.

For Cassowary, the simplex tableau has to be prepared for incremental re-solving, and all variables that will be assigned have to be known beforehand. This preparation is potentially slow, and it is not possible with the implementation of the algorithm to keep multiple optimized versions of the tableau around. Thus, the heuristic we use for Cassowary is more akin to a JIT: for each variable known to Cassowary, we keep a counter that tracks how often the variable has been assigned recently. In regular intervals, we check which n variables were assigned to most frequently, and optimize the tableau

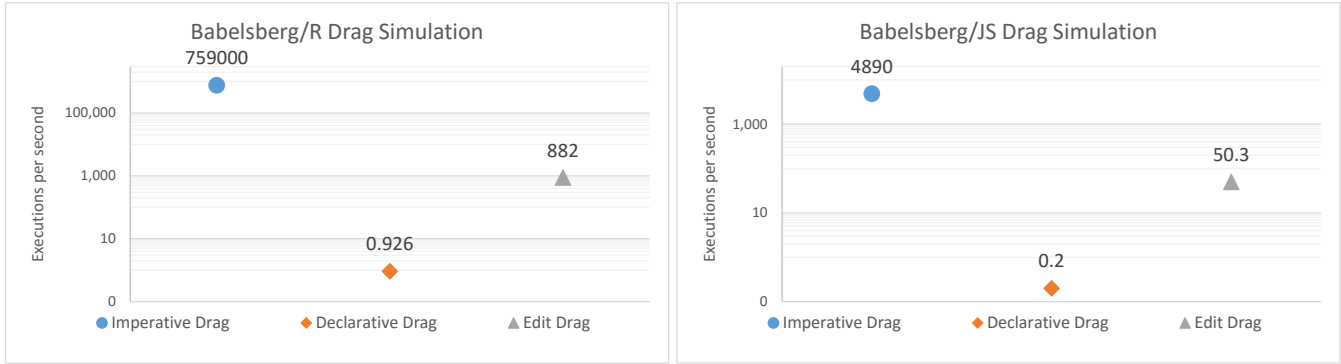


Figure 1: A comparison of constraint solving performance for hand-coded imperative solving, Babelsberg-style solving through assignment, and Babelsberg with edit constraints. Numbers show how many re-solving operations can be executed per second (more is better).

for changes coming from those variables. At the same time, we “decay” the counters either by a fixed percentage or value. This ensures that variables that have been assigned to a lot in the past, but not much in the recent history of the program, are no longer considered for incremental re-satisfaction.

Benchmark Results

We present two sets of benchmarks, one each for DeltaBlue and Cassowary, in Figure 2. In our benchmarks, we measure a chain of variables that should be equal to a fixed sum, a horizontal drag of a slider where only one variable changes, a mouse drag where two variables changes alternate, a mouse drag where one dimension changes more frequently than the other, and finally a mouse drag where each dimension changes five times, and then the other changes five times.

For DeltaBlue, the best heuristic is to keep the last edit constraint, in a strategy we call *Last JIT*. At any time, if there is no current edit constraint, we create one. If the current edit constraint is for another variable, we throw the old one away and create the new one. This implementation could easily be extended to cache the last n edit constraints, rather than just the last one. However, even as it is, we can see in our benchmark that this heuristic is almost always as fast as writing edit constraints directly, and is never slower than not using edit constraints.

For Cassowary, we include three heuristics with Babelsberg: the *Classic JIT* strategy decays counters and changes or creates edit constraints in fixed intervals. A second strategy, *Additive Adaptive*, increments the interval any time the most frequently used variable did not change, and decrements the interval any time it did. Thus, when an edit constraint is well chosen and can stay in effect for a long time, we reduce the overhead of checking and decaying counters linearly with time. A third strategy, *Multiplicative Adaptive*, modifies this behavior and, rather than incrementing or decrementing the interval, it multiplies or divides the interval by two. This has the advantage that we can avoid re-checks for longer periods of time if the edit constraint stays in effect.

Our benchmarks show that all our heuristics are faster than using no edit constraints at all. The adaptive strategies generally work better than the *Classic JIT* strategy, and by default we use the *Additive Adaptive* strategy, but the developer can select a different strategy manually.

5. Related Work

There is some related work for automatic solver selection in other constraint programming systems. Both Sketchpad [22] and

ThingLab [2] used the same three hard-wired solvers (a relaxation solver, propagation of degrees of freedom, and local propagation). However, since the list of solvers was fixed and their capabilities have little overlap, the selection algorithm did not need to be general. Similarly, the Kaleidoscope [15] and Turtle [13] constraint-programming systems only had a fixed set of low-level constraint solvers, and a fixed algorithm for calling user-defined solving methods.

SMT solvers like Z3 [4] include many different solving strategies for different types of problems and use a standard algorithm to have these strategies cooperate. However, most SMT solvers require manual selection of the solving strategy if performance or solution quality is important and only use a fixed, generic strategy based on type heuristics otherwise.

Lighthouse [21] is a system for selecting the fastest constraint solver for a given problem. The system itself is designed to support different heuristics and its general direction is thus similar to our heuristics-based solver selection. However, Lighthouse is a separate tool to aid high-performance computing application developers during development, whereas we propose at least a limited form of automatic solver selection to be used at runtime.

We are not aware of work that applies just-in-time techniques to constraint solvers, but there is a large body of work in scientific computing to pre-select optimized sparse matrix kernels for use by linear solvers to optimize performance in HPC systems such as ATLAS [26], OSKI [25], SALSALSA [5], and many more. The major difference to our approach and goals are that these systems are all targeted towards HPC applications. In these applications analysis and tuning may take a long time (and is usually done before the actual computation). In Babelsberg, on the other hand, recognizing the conditions for edit constraints and applying them has to happen at runtime and is thus subject to the same issues as traditional JITs that must weigh the performance gain of an optimization against the performance impact of analyzing and enabling it.

6. Conclusions

We have presented the different implementation approaches for automatic solver selection used in the Babelsberg implementations and how they can aid imperative developers employ constraint solving successfully. In addition, we have presented a novel application of JIT-techniques to incremental re-solving in the DeltaBlue and Cassowary constraint solvers which in many cases can offer one order of magnitude performance improvements over a naïve formulation of the constraints, and often comes close the performance of manually applied edit constraints.

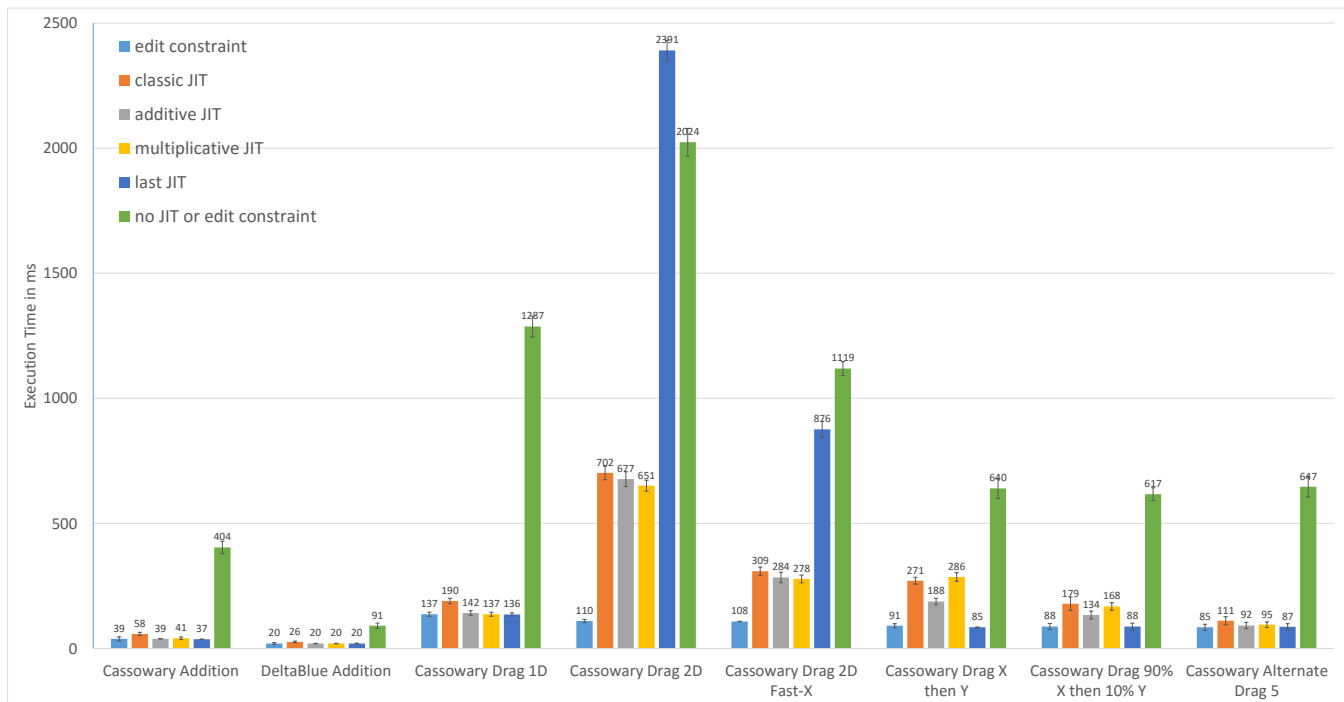


Figure 2: Combinations of benchmarks and automatic edit constraint JITs. Graph shows execution time required for 500 solving operations (less is better).

For the automatic selection, in practice we have found a mixture of manual and eager selection to produce good results once the user has a basic understanding of the available solvers and is aware of the eager selection process (in particular, how seemingly idempotent refactorings may lead to different results). We have found that while preferential selection avoids some surprising behavior, this behavior occurs rarely in practice. The heuristic solver selection procedure, although very powerful, has strong drawbacks: its complexity impacts the performance of creating new constraints, and requires constant re-checking. As with any heuristic, the results also depend on the weight that is given to each of the metrics and may need to be adjusted depending on the application domain. An educational advantage, however, is that practical implementations can use the metrics to communicate to the user the selection process and increase the user’s understanding of the capabilities and limits of available constraint solvers. As a guideline to implementers, we suggest using the heuristic procedure as an educational tool and guiding instrument at development-time, but revert to manual and eager selection when many constraints are added dynamically throughout the run-time of the program, to avoid the performance overhead of the selection procedure.

In future work, we plan to extend the heuristics in the practical implementations and provide more principled criteria based on our practical experience for using a specific selection strategy, and for weighing the different heuristics against one another.

Regarding our automatic edit constraints, more work is required to determine good heuristics for selecting the appropriate JIT strategy in many cases. However, we argue that the work presented here is a good first step in the direction of improving solver performance, and has applications outside of the domain of object-constraint programming languages.

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